Static Program Analysis Part 9 – pointer analysis

http://cs.au.dk/~amoeller/spa/

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Agenda

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

Analyzing programs with pointers

How do we perform e.g. constant propagation analysis when the programming language has pointers? (or object references?)

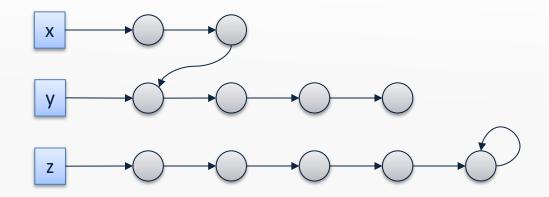
```
*x = 42;
*y = -87;
z = *x;
// is z 42 or -87?
```

$$S \rightarrow *X = E;$$
| ...

$$E \rightarrow E(E, ..., E)$$

Heap pointers

- For simplicity, we ignore records
 - alloc then only allocates a single cell
 - only linear structures can be built in the heap



- Let's at first also ignore function pointers
- We still have many interesting analysis challenges...

Pointer targets

- The fundamental question about pointers:
 What locations can they point to?
- We need a suitable abstraction
- The set of (abstract) cells, Cells, contains
 - alloc-i for each allocation site with index i
 - X for each program variable named X
- This is called allocation site abstraction
- Each abstract cell may correspond to many concrete memory cells at runtime

Points-to analysis

- Determine for each pointer variable X the set pt(X) of the cells X may point to
- A conservative ("may points-to") analysis:
 - the set may be too large
 - can show absence of aliasing: $pt(X) \cap pt(Y) = \emptyset$
- We'll focus on flow-insensitive analyses:
 - take place on the AST
 - before or together with the control-flow analysis

*x = 42:

*y = -87;

// is z 42 or -87?

Obtaining points-to information

- An almost-trivial analysis (called address-taken):
 - include all alloc-i cells
 - include the X cell if the expression &X occurs in the program
- Improvement for a typed language:
 - eliminate those cells whose types do not match
- This is sometimes good enough
 - and clearly very fast to compute

Pointer normalization

- Assume that all pointer usage is normalized:
 - X = alloc P where P is null or an integer constant
 - X = &Y
 - X = Y
 - X = *Y
 - *X = Y
 - X = null
- Simply introduce lots of temporary variables...
- All sub-expressions are now named
- We choose to ignore the fact that the cells created at variable declarations are uninitialized

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Andersen's analysis (1/2)

- For every cell c, introduce a constraint variable $[\![c]\!]$ ranging over sets of locations, i.e. $[\![\cdot]\!]$: Cells $\to 2^{Cells}$
- Generate constraints:

•
$$X = \text{alloc } P$$
: alloc- $i \in [X]$

•
$$X = \&Y$$
: $Y \in \llbracket X \rrbracket$

•
$$X = Y$$
: $[Y] \subseteq [X]$

•
$$X = {}^*Y$$
: $\alpha \in [Y] \Rightarrow [\alpha] \subseteq [X]$ for each $\alpha \in Cells$

• *
$$X = Y$$
: $\alpha \in [X] \Rightarrow [Y] \subseteq [\alpha]$ for each $\alpha \in Cells$

•
$$X = null$$
: (no constraints)

Andersen's analysis (2/2)

The points-to map is defined as:

$$pt(X) = [X]$$

- The constraints fit into the cubic framework ©
- Unique minimal solution in time $O(n^3)$
- In practice, for Java: $O(n^2)$
- The analysis is flow-insensitive but directional
 - models the direction of the flow of values in assignments

Example program

```
var p,q,x,y,z;
p = alloc null;
x = y;
X = Z;
*p = z;
p = q;
q = &y;
x = *p;
p = \&z;
```

Applying Andersen

Generated constraints:

```
alloc-1 \in [p]
[y] \subseteq [x]
[z] \subseteq [x]
\alpha \in [p] \Rightarrow [z] \subseteq [\alpha]
[q] \subseteq [p]
y \in [q]
\alpha \in [p] \Rightarrow [\alpha] \subseteq [x]
z \in [p]
```

Smallest solution:

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Steensgaard's analysis

- View assignments as being bidirectional
- Generate constraints:

•
$$X = \text{alloc } P$$
: $\text{alloc-} i \in [X]$

•
$$X = \&Y$$
: $Y \in \llbracket X \rrbracket$

•
$$X = Y$$
: $[X] = [Y]$

•
$$X = *Y$$
: $\alpha \in [Y] \Rightarrow [\alpha] = [X]$

•
$$*X = Y$$
: $\alpha \in [X] \Rightarrow [Y] = [\alpha]$

Extra constraints:

 $t_1, t_2 \in [\![t]\!] \Rightarrow [\![t_1]\!] = [\![t_2]\!]$ and $[\![t_1]\!] \cap [\![t_2]\!] \neq \emptyset \Rightarrow [\![t_1]\!] = [\![t_2]\!]$ (whenever a cell may point to two cells, they are effectively merged into one)

• Steensgaard's original formulation uses conditional unification for X = Y: $\alpha \in [Y] \Rightarrow [X] = [Y]$ (avoids unifying if Y is never a pointer)

Steensgaard's analysis

- Reformulate as term unification
- Generate constraints:

•
$$X = alloc P$$
: $||X|| = &||alloc - i||$

•
$$X = \&Y$$
: $[X] = \&[Y]$

•
$$X = Y$$
: $[X] = [Y]$

•
$$X = *Y$$
: $[Y] = & \alpha \land [X] = \alpha$ where α is fresh

•
$$*X = Y$$
: $[X] = & \alpha \land [Y] = \alpha \text{ where } \alpha \text{ is fresh}$

- Terms:
 - term variables, e.g. [X], [alloc-i], α (each representing the possible values of a cell)
 - a single (unary) term constructor &t (representing the location of the cell that t represents)
 - $\|X\|$ is now a term variable, not a constraint variable holding a set of cells
- Fits with our unification solver! (union-find...)
- The points-to map is defined as pt(X) = { c∈Cells | [[X]] = & [[c]] }
- Note that there is only one kind of term constructor, so unification never fails₁₆

Applying Steensgaard

Generated constraints:

```
alloc-1 \in [p]
[y] = [x]
[z] = [x]
\alpha \in [\![p]\!] \Rightarrow [\![z]\!] = [\![\alpha]\!]
[q] = [p]
y \in [q]
\alpha \in \llbracket p \rrbracket \Rightarrow \llbracket \alpha \rrbracket = \llbracket x \rrbracket
z \in [p]
+ the extra constraints
```

• Smallest solution:

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Interprocedural points-to analysis

- If function pointers are distinct from heap pointers:
 - first run a CFA
 - then run Andersen or Steensgaard
- But in TIP both kinds may be mixed together:

$$(***x)(1,2,3)$$

• In this case the CFA and the points-to analysis must happen *simultaneously*!

Function call normalization

Assume that all function calls are of the form

$$x = y(a_1, ..., a_n)$$

- y may be a variable whose value is a function pointer
- Assume that all return statements are of the form

- As usual, simply introduce lots of temporary variables...
- Include all function names in Cells

CFA with Andersen

For the function call

$$x = y(a_1, ..., a_n)$$

and every occurrence of

Andersen's analysis is already closely connected to control-flow analysis!

 $f(x_1, ..., x_n)$ { ... return z; } add these constraints:

$$f \in \llbracket f \rrbracket$$
 $f \in \llbracket y \rrbracket \Rightarrow (\llbracket a_i \rrbracket \subseteq \llbracket x_i \rrbracket \text{ for i=1,...,} n \land \llbracket z \rrbracket \subseteq \llbracket x \rrbracket)$

- (Similarly for simple function calls)
- Fits directly into the cubic framework!

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Null pointer analysis

- Decide for every dereference *p, is p different from null?
- Use the monotone framework
 - assuming that a points-to map pt has been computed
- Let us consider an intraprocedural analysis
 (i.e. we ignore function calls)

A lattice for null analysis

Define the simple lattice Null:



where NN represents "definitely **n**ot **n**ull" and ? represents "maybe null"

Use for every program point the map lattice:

Cells
$$\rightarrow$$
 Null

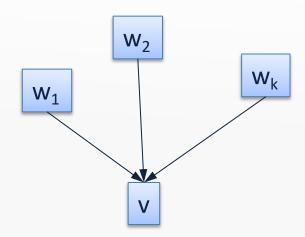
Setting up

- For every CFG node, v, we have a variable [[v]]:
 - a map giving abstract values for all cells at the program point after v
- Auxiliary definition:

$$JOIN(v) = \coprod [w]$$

 $w \in pred(v)$

(i.e. we make a *forward* analysis)



For operations involving pointers:

- For all other CFG nodes:
 - [[v]] = *JOIN*(v)

- For a heap store operation *X = Y we need to model the change of whatever X points to
- That may be multiple abstract cells pointed to by X
 (i.e. the cells pt(X))
- With the present abstraction, each abstract heap cell alloc-i may des Weak updates cannot "kill"
- So we settle for \mathbf{v} information flowing into a node *X = Y: $[\![\mathbf{v}]\!] = store(JOIN(\mathbf{v}), X, Y)$

where
$$store(\sigma, X, Y) = \sigma[\alpha \mapsto \sigma(\alpha) \sqcup \sigma(Y)]$$

- For a heap load operation $X = {}^*Y$ we need to model the change of the program variable X
- Our abstraction has a single abstract cell for X
- That abstract ce Strong updates can "kill"
- So we can use s information flowing into a node

$$X = *Y$$
: $\llbracket v \rrbracket = load(JOIN(v), X, Y)$

where
$$load(\sigma, X, Y) = \sigma[X \mapsto \bigcup \sigma(\alpha)]$$

Strong and weak updates

```
mk() {
  return alloc null; // alloc-1
a = mk();
b = mk();
*a = alloc null; // alloc-2
n = null;
*b = n; // strong update here would be unsound!
c = *a;
```

is C null here?

The abstract cell alloc-1 corresponds to multiple concrete cells

Strong and weak updates

```
a = alloc null; // alloc-1
b = alloc null; // alloc-2
*a = alloc null; // alloc-3
*b = alloc null; // alloc-4
if (...) {
 x = a;
} else {
  x = b;
n = null;
*x = n; // strong update here would be unsound!
c = *x;
```

is **C** null here?

The points-to set for x contains *multiple abstract cells*

```
    X = alloc P: [v] = JOIN(v)[X → NN, alloc-i → ?]
    X = &Y: [v] = JOIN(v)[X → NN]
    X = Y: [v] = JOIN(v)[X → JOIN(v)(Y)]
    X = null: [v] = JOIN(v)[X → ?]
```

- In each case, the assignment modifies a program variable each with a unique cell
- So we can use strong updates, as for heap load operations

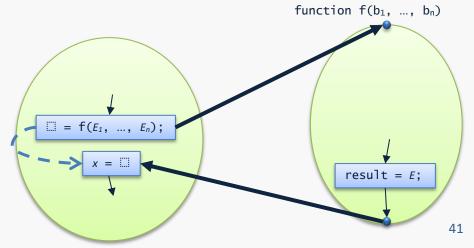
Strong and weak updates, revisited

- Strong update: $\sigma[c \mapsto new-value]$
 - possible if c is known to refer to a single concrete cell
 - works for assignments to local variables
 (as long as TIP doesn't have e.g. nested functions)

- Weak update: $\sigma[c \mapsto \sigma(c) \sqcup new-value]$
 - necessary if c may refer to multiple concrete cells
 - bad for precision, we lose some of the power of flow-sensitivity
 - required for assignments to heap cells (unless we extend the analysis abstraction!)

Interprocedural null analysis

- Context insensitive or context sensitive, as usual...
 - at the after-call node, use the heap from the callee
- But be careful!
 Pointers to local variables may escape to the callee
 - the abstract state at the after-call node cannot simply copy the abstract values for local variables from the abstract state at the call node



Using the null analysis

The pointer dereference *p is "safe" at entry of v if
 JOIN(v)(p) = NN

• The quality of the null analysis depends on the quality of the underlying points-to analysis

Example program

```
p = alloc null;
q = &p;
n = null;
*q = n;
*p = n;
```

Andersen generates:

```
pt(p) = {alloc-1}
pt(q) = {p}
pt(n) = Ø
```

Generated constraints

Solution

- At the program point before the statement *q=n
 the analysis now knows that q is definitely non-null
- ... and before *p=n, the pointer p is maybe null
- Due to the weak updates for all heap store operations, precision is bad for alloc-i locations

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Points-to graphs

- Graphs that describe possible heaps:
 - nodes are abstract cells
 - edges are possible pointers between the cells
- The lattice of points-to graphs is $2^{Cells \times Cells}$ ordered under subset inclusion (or alternatively, $Cells \rightarrow 2^{Cells}$)
- For every CFG node, v, we introduce a constraint variable \[v\] describing the state after v
- Intraprocedural analysis (i.e. ignore function calls)

Constraints

For pointer operations:

```
• X = \text{alloc } P: [v] = JOIN(v) \downarrow X \cup \{ (X, \text{alloc} - i) \}

• X = \&Y: [v] = JOIN(v) \downarrow X \cup \{ (X, Y) \}

• X = Y: [v] = assign(JOIN(v), X, Y)

• X = *Y: [v] = load(JOIN(v), X, Y)

• *X = Y: [v] = store(JOIN(v), X, Y)

• X = \text{null}: [v] = JOIN(v) \downarrow X
```

- For all other CFG nodes:

Auxiliary functions

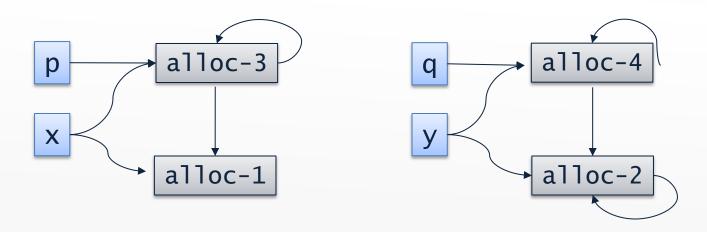
- $JOIN(v) = \bigcup_{w \in pred(v)} [w]$
- $\sigma \downarrow X = \{ (s,t) \in \sigma \mid s \neq X \}$
- $assign(\sigma, X, Y) = \sigma \downarrow X \cup \{ (X, t) \mid (Y, t) \in \sigma \}$
- $load(\sigma, X, Y) = \sigma \downarrow X \cup \{ (X, t) \mid (Y, s) \in \sigma, (s, t) \in \sigma \}$
- $store(\sigma, X, Y) = \sigma \cup \{(s, t) \mid (X, s) \in \sigma, (Y, t) \in \sigma\}$
 - note: weak update!

Example program

```
var x,y,n,p,q;
x = alloc null; y = alloc null;
*x = null; *y = y;
n = input;
while (n>0) {
  p = alloc null; q = alloc null;
  *p = x; *q = y;
 x = p; y = q;
 n = n-1;
```

Result of analysis

After the loop we have this points-to graph:



We conclude that x and y will always be disjoint

Points-to maps from points-to graphs

A points-to map for each program point v:

$$pt(X) = \{ t \mid (X,t) \in [\![v]\!] \}$$

- More expensive, but more precise:
 - Andersen: $pt(x) = \{ y, z \}$
 - flow-sensitive: $pt(x) = \{z\}$

```
x = &y;
x = &z;
```

Improving precision with abstract counting

- The points-to graph is missing information:
 - alloc-2 nodes always form a self-loop in the example
- We need a more detailed lattice:

$$2^{Cell \times Cell} \times (Cell \rightarrow Count)$$

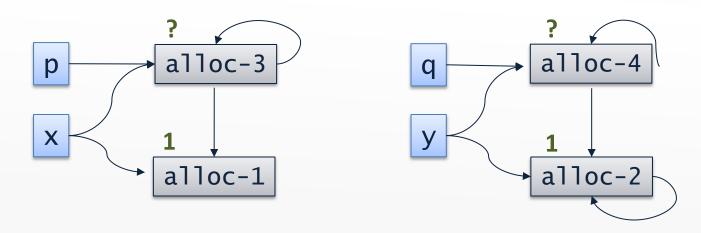
where we for each cell keep track of how many concrete cells that abstract cell describes

$$Count = 0 1 >1$$

 This permits strong updates on those that describe precisely 1 concrete cell

Better results

After the loop we have this extended points-to graph:



Thus, alloc-2 nodes form a self-loop

Escape analysis

- Perform a points-to analysis
- Look at return expression
- Check reachability in the points-to graph to arguments or variables defined in the function itself

None of those

no escaping stack cells

```
baz() {
  var x;
  return &x;
main() {
  var p;
  p=baz();
  *p=1;
  return *p;
```